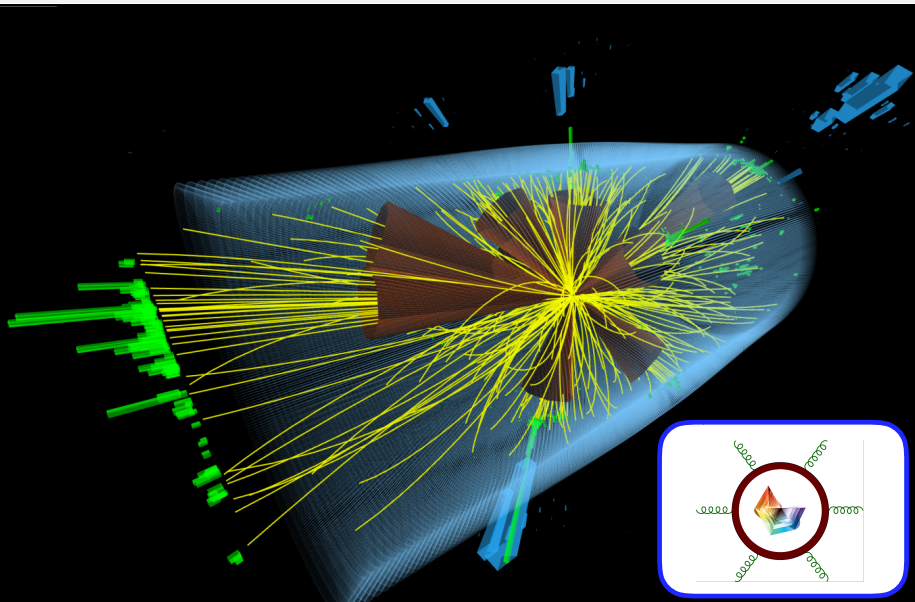


# Pushing the Boundaries of Collider Physics with Jet Substructure

Ian Mout  
Yale



# Jets at the LHC

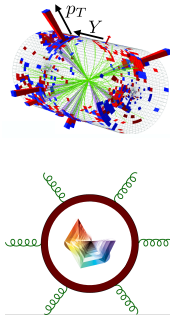
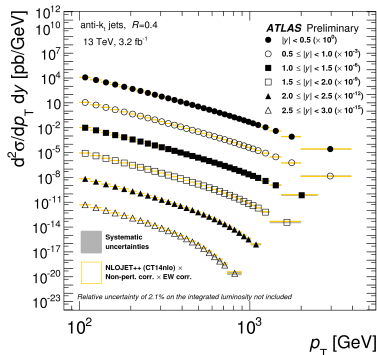




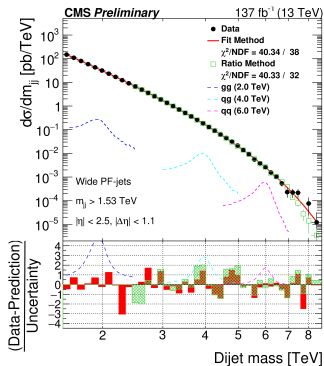
# Jets at the LHC

- Obtaining a precise description of jet cross sections has been a significant **driver of theory developments** in Quantum Field Theory.

## Jet Kinematic Distributions

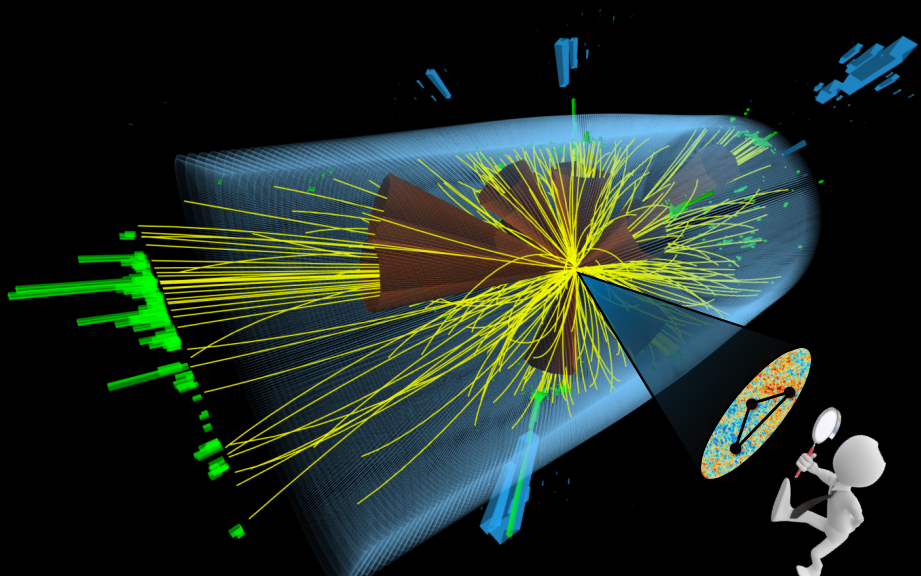


## Dijet Mass



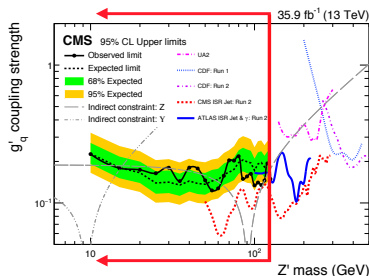
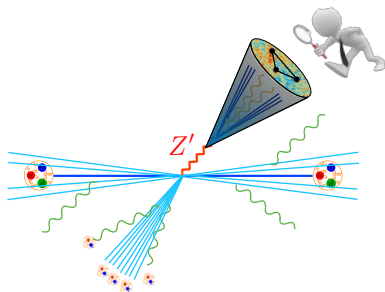
- Enables precision **tests of QCD** and **searches for new physics**.

# Jet Substructure!



# Jet Substructure: Searches

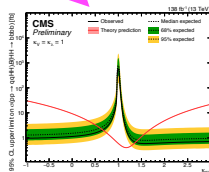
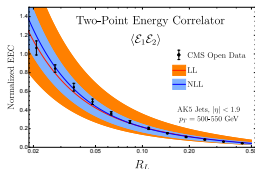
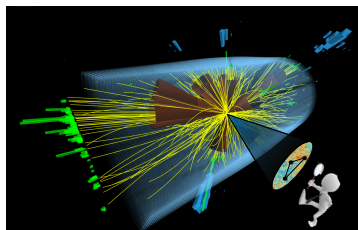
- **Jet Substructure** uses the internal structure of jets to provide **qualitatively new** ways to study physics at colliders.



- Its introduction in 2008 by **Butterworth, Davison, Rubin and Salam**, along with anti- $k_T$  by **Cacciari, Soyez, Salam** reinvigorated the study of jets in QCD.

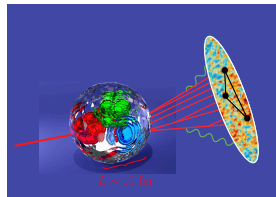
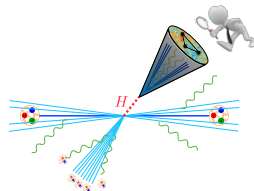
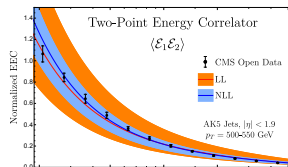
# The Boundaries of Collider Physics

- Progress in **formal theory** and **data science** have transformed jet substructure, enabling **new tests of QFT**, and **ever improving ways to search for fundamental physics**.

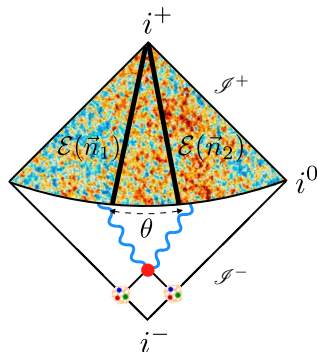
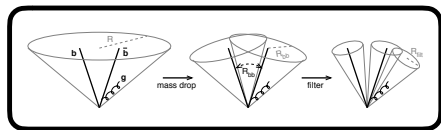


# Outline

- Field Theoretic Foundations and Precision Jet Substructure
- Data Science and Searches
- The Frontiers of QCD



# From Phenomenological Procedures to Field Theoretic Observables

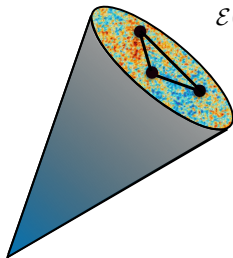


# Insights from Conformal Field Theory

- Motivated by the phenomenological importance of jet substructure, one can give it a **proper field theoretic foundation**. [Kravchuk, Simmons-Duffin] [Hofman, Maldacena]
- Achieved through the introduction of **light-ray operators**. [Korchemsky, Sterman]

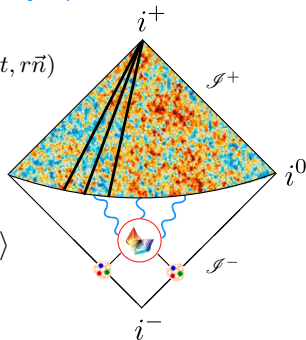


[Basham, Brown, Ellis, Love]



$$\mathcal{E}(\vec{n}) = \lim_{r \rightarrow \infty} r^2 \int_0^\infty dt n^i T_{0i}(t, r\vec{n})$$

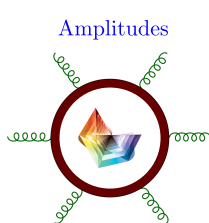
$$\langle \Psi | \mathcal{E}(\hat{n}_1) \cdots \mathcal{E}(\hat{n}_k) | \Psi \rangle$$



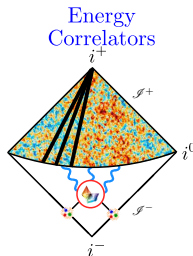
- From the perspective of QFT, jet substructure is the study of correlation functions of energy flow operators.

# Energy Correlators

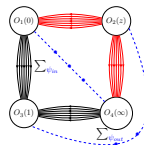
- Correlation functions of energy flow operators take an interesting intermediate position between amplitudes and correlation functions.



Asymptotic  
States



Correlation  
Functions



IR Finite



- Calculating physical observables in QFT has traditionally been a fruitful approach to developing a deeper understanding.

[Dixon et al.]  
[Yan, Zhang]  
[Belitsky et al.]

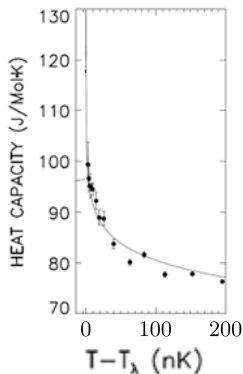
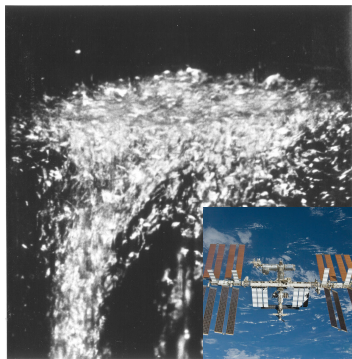


# Scaling Behavior in QFT

- Why is jet substructure theoretically interesting?
- QFTs exhibit universal behavior as operators are brought together.



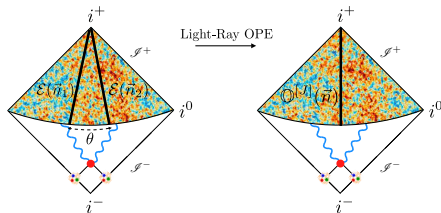
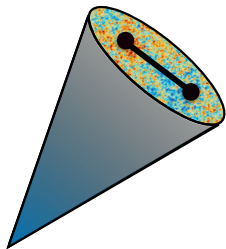
## $\lambda$ -point of Helium



$$\mathcal{O}(x)\mathcal{O}(0) = \sum x^{\gamma_i} c_i \mathcal{O}_i$$

# The OPE Limit of Lightray Operators

- Energy flow operators also admit an OPE!
- The substructure of jets is determined by the OPE structure of lightray operators.



$$\mathcal{E}(\hat{n}_1)\mathcal{E}(\hat{n}_2) \sim \sum \theta^{\tau_i-4} \mathbb{O}_i(\hat{n}_1)$$

[Hofman, Maldacena]

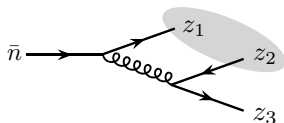
[Chang, Kologlu, Kravchuk, Simmons Duffin, Zhiboedov]

[See Also: Konishi, Ukawa, Veneziano]

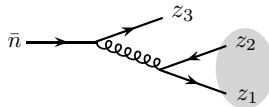
- Progress in CFT provided an understanding of the  $\mathbb{O}_i$  in the OPE.
- Allows a reformulation of jet substructure as the study of the symmetry and OPE structure of these operators.

# Connecting Fields

- Provides a direct connection between recent developments in (Lorentzian) CFT and real world collider physics!



**Snowmass White Paper:  
The Analytic Conformal Bootstrap**



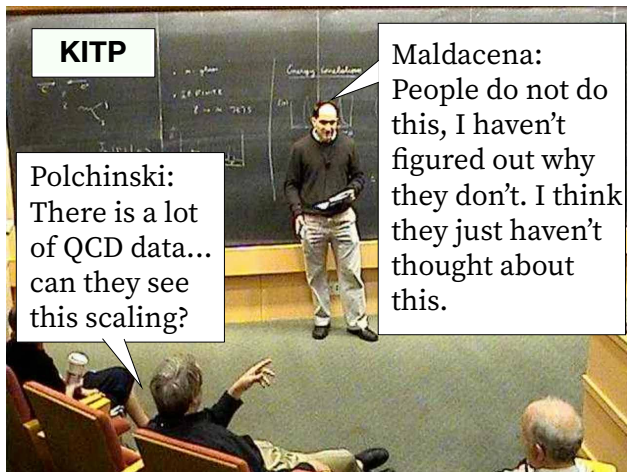
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Thomas Hartman,<sup>1</sup> Dalimil Mazáč,<sup>2</sup> David Simmons-Duffin,<sup>3</sup> Alexander Zhiboedov<sup>4</sup>

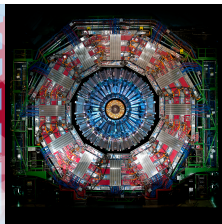
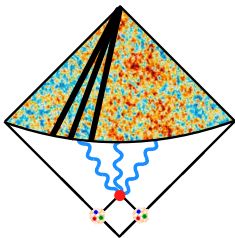
Remarkably, the machinery of the OPE [49, 65, 71, 72] and crossing equations [24, 25] can be generalized to light-ray operators in a nontrivial way. The light-ray OPE has interesting applications in the study of jet substructure in QCD [73, 74]. Developing a better understanding of the space of light-ray operators and associativity of the light-ray OPE is an important open problem in our quest for understanding nonperturbative Lorentzian dynamics of CFTs.

- Perturbative data from Jet Substructure calculations has played an important role in developing the light-ray OPE.

# Theory-Experiment Gap



# Open Data as the Bridge Between Theory and Experiment



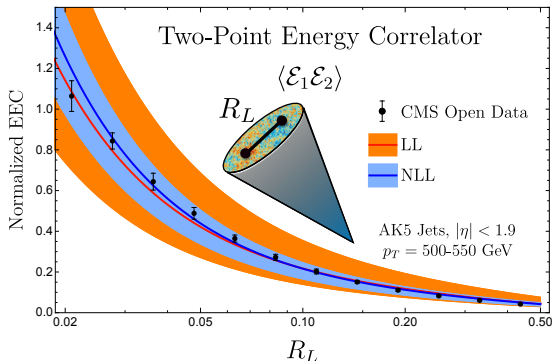
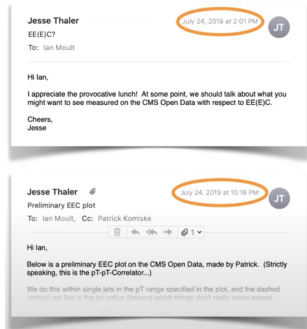
# Open Data

- A primary driver of recent progress in jet substructure has been the availability of Open Data.



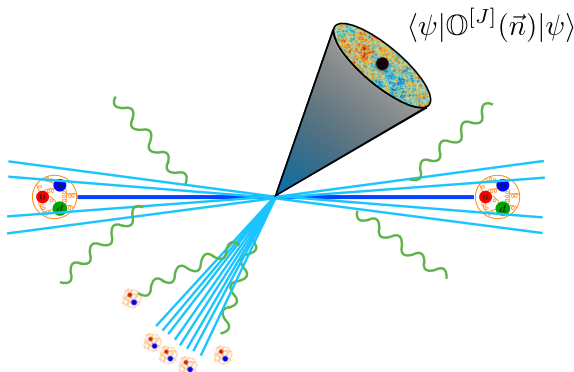
- Short-circuits the traditional path from formal theory development to collider physics applications:
  - Enables rapid transport of ideas from “theory world” to “real world”.
  - Can illustrate that new approaches are phenomenologically viable.
  - Provides tests on real data for observables where standard simulations can't be trusted  $\Rightarrow$  learn new features of QCD.

- Open Data in Action: The  $\mathcal{E}(\hat{n}_1)\mathcal{E}(\hat{n}_2)$  OPE inside high-energy jets!



- An observable **never before considered in LHC jets**, can be analyzed from scratch in one afternoon, and used to verify a **never before tested OPE in QFT!** And initiate a new direction in Jet Substructure!

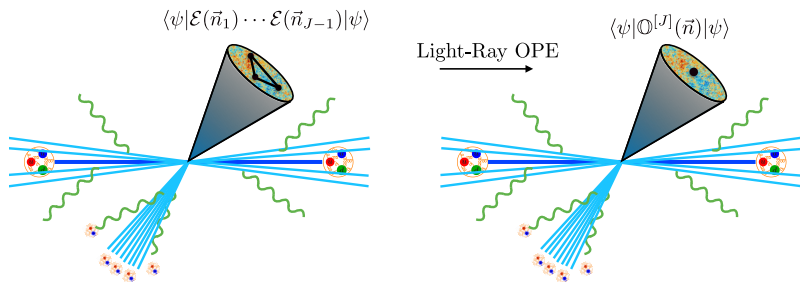
# Jet Substructure as a Precision Science





# Precision Jet Substructure

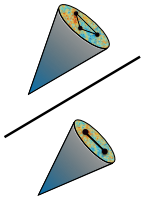
- Reformulation in terms of **field theoretic operators** allows one to **replace heuristic jet shapes** with sharp probes of the underlying theory:
  - 1 Directly **relates observables and field theoretic quantities**.
  - 2 Opens the door to the use of techniques from **formal theory for calculations in collider environments**.

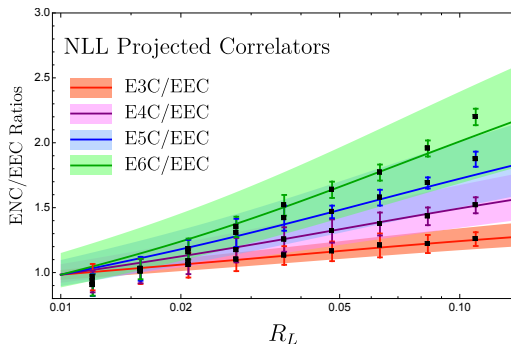


# The Spectrum of a Jet

[Chen, Moulton, Zhang, Zhu]  
[Lee, Mehta, Moulton]

- Measurements of asymptotic energy flux directly extract the **spectrum of (twist-2) lightray operators** in QCD **at the quantum level!**

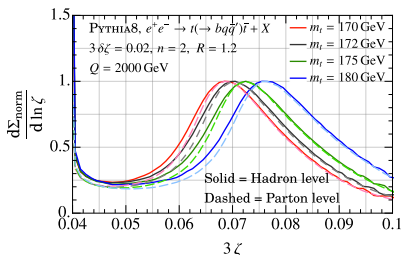
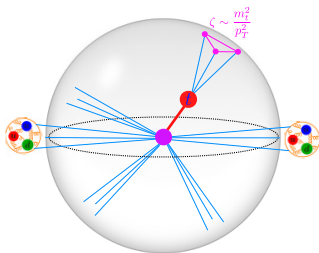

$$\frac{\langle \mathcal{E}_1 \mathcal{E}_2 \cdots \mathcal{E}_{J-1} \rangle}{\langle \mathcal{E}_1 \mathcal{E}_2 \rangle} \sim \frac{\langle \mathcal{O}^{[J]} \rangle}{\langle \mathcal{O}^{[3]} \rangle}$$



- A **never before observed feature of QFT**, accessible due to the high energies and remarkable detectors of the LHC.

# Application I: Top Quark Mass Measurement

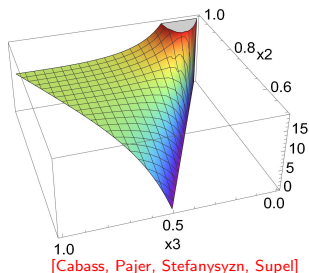
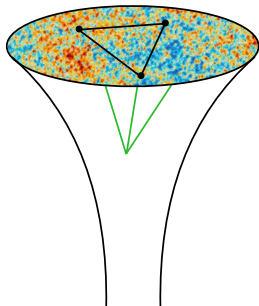
- The **top quark mass** is a central parameter of the SM.
- Mass measurements are subtle: **need observables with top mass sensitivity that can be computed from first principles field theory.**
- Massive particles break the scaling of the correlators and **imprint their existence at a characteristic angular scale  $\zeta \sim m_t^2/Q^2$ .**



- **Optimistic for a precision ( $\lesssim 1 \text{ GeV}$ ) top mass extraction at LHC from jet substructure!** [Holguin, Moul, Pathak, Procura]

# Shape Dependence

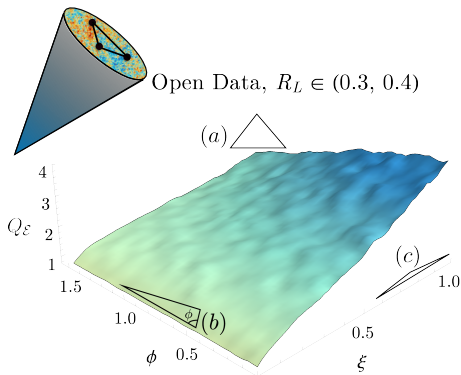
- Scaling probes the spectrum, but **higher-point correlators probe more detailed aspects of interactions.**
- e.g. Non-Gaussianities allow one to distinguish models of inflation.



- Can we compute higher-point functions of energy flux?

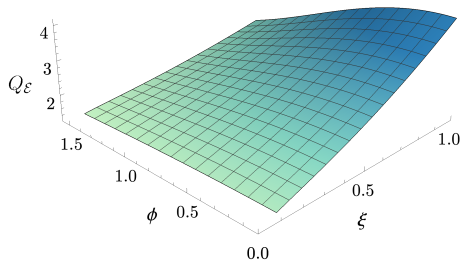
# Shape Dependence of Non-Gaussianities in Data

- Can directly study non-gaussianities inside high energy jets.



$$G_{N,LL}(z) = \frac{1+u+v}{2uv}(1+\zeta_2) - \frac{1+u}{2uv}\log(u) - \frac{1+v}{2uv}\log(v) \\ - (1+u+v)(\partial_u + \partial_v)\Phi(z) + \frac{(1+u^2+v^2)}{2uv}\Phi(z) + \frac{(z-z^2)(u+v+u^2+v^2+u^2v+uv^2)}{4u^2v^2}\Phi(z) \\ + \frac{(u-1)(u+1)}{2uv^2}D_2^*(z) + \frac{(v-1)(v+1)}{2u^2v}D_2^*(1-z) + \frac{(u-v)(u+v)}{2uv}D_2^*\left(\frac{z}{z-1}\right)$$

LL + LO prediction,  $R_L = 0.35$

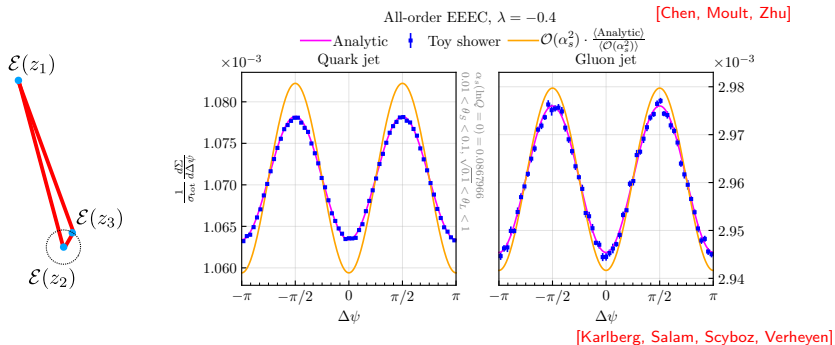


[Chen, Moul, Thaler, Zhu]

- Illustrates theoretical control over multi-point correlations!

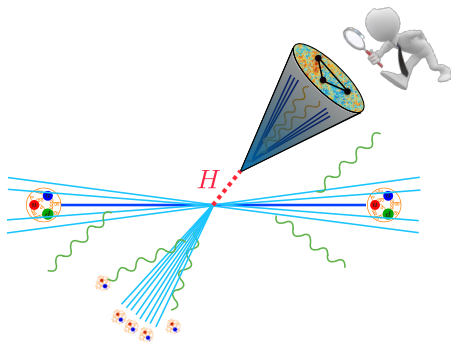
# Application II: Parton Shower Development

- Illustrates complete control of three-point correlations in jets.
- Crucial for validating implementations of higher order effects in parton showers. e.g. Spin Correlations (transverse spin operators)



- Full incorporation of higher-point correlations in parton showers plays an important role in enhancing the LHC search program.

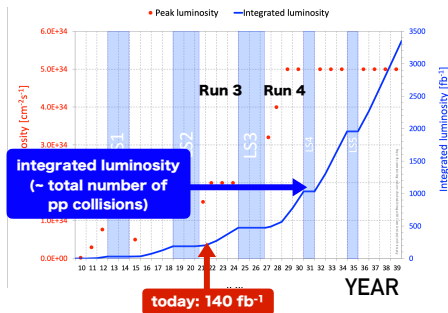
# Fundamental Physics from QCD + Machine Learning



# Jet Substructure: Searches

- The combination of an improved description of the “fine structure” of jets and modern Machine Learning continues to **drive innovative search strategies at the LHC**.
- Jet Substructure will benefit immensely from the population of ever more extreme phase space regions with high luminosity.

- Luminosity is only a relevant metric if no one learns anything between now and 2040.

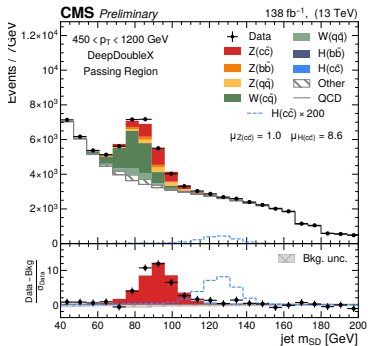
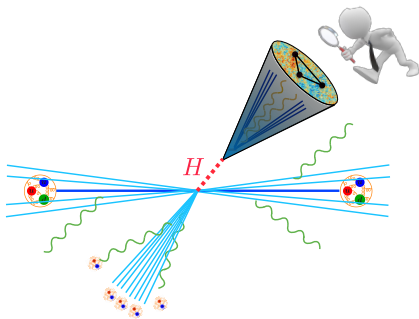


Gavin P. Salam



# Jet Substructure: Searches

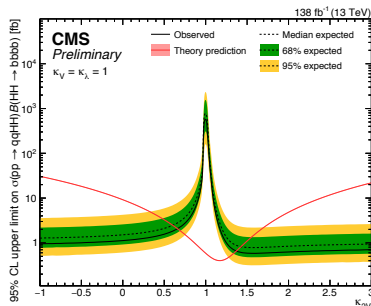
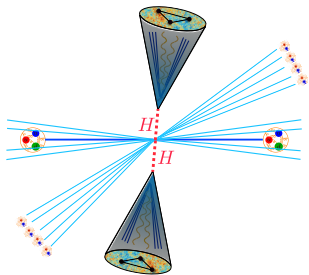
- Measurements of the **Higgs couplings to light quarks** provide a crucial test of the **Yukawa sector of the SM**.
- Jet substructure (ParticleNet) provides the current **most stringent bound on the charm Yukawa**,  $1.1 < \kappa_c < 5.5$ .



- Matches the original projected sensitivity with 3000 fb<sup>-1</sup>!

# Jet Substructure: Searches

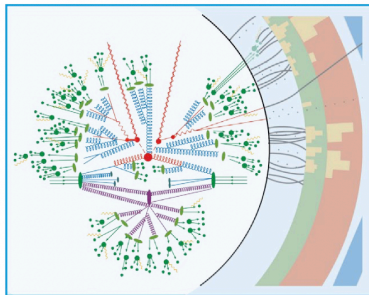
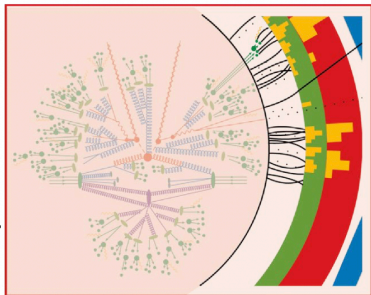
- The **Higgs self interaction** accesses the Higgs potential.
- Jet Substructure exploits the high branching ratio to b-quarks.



- First observation of the  $VV \rightarrow HH$  coupling in the SM!

# Machine Learning for Quantum Chromodynamics

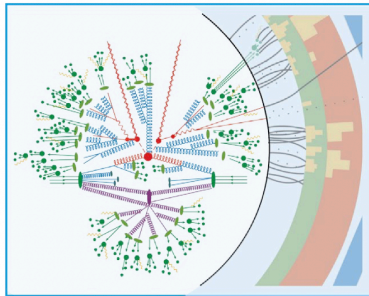
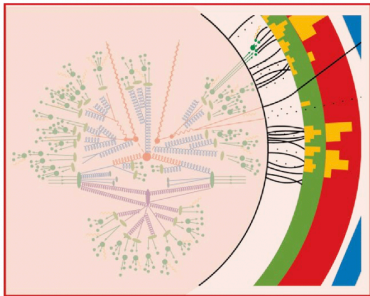
Credit: Benjamin Nachman



# From Detector Data to Theory Comparisons

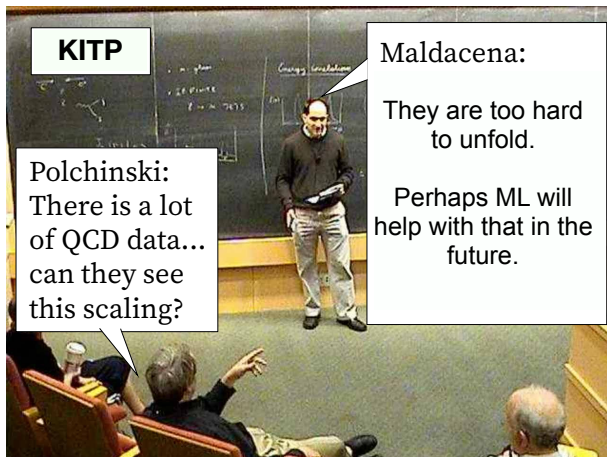
- To be interpreted theoretically, measurements must “invert” the effects of the detector: [Unfolding](#).
- “Simple” if one projects to low dimensional features such as jets.
- To measure statistical properties of energy flux requires [unfolding the full particle phase space](#).

Credit: Benjamin Nachman



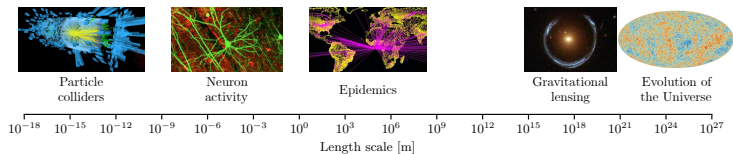
# Theory-Experiment Gap

- The extraordinary complexity of the LHC dataset, has produced a gap between what theorists want, and what can be measured.



# Likelihood Free Inference

- Traditional approaches to unfolding that explicitly determine the likelihood fail:
  - High dimensional input space - full phase space of detector effects.
  - High dimensional output space - space of energy correlations.
- This is a common feature of many modern data sets in the physical sciences, for which we have high fidelity simulations:  
⇒ rapidly developing field of “Likelihood Free Inference”

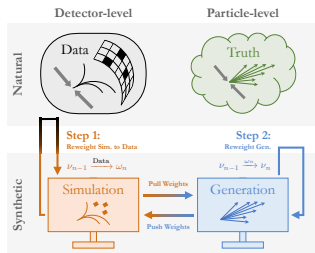


[Cranmer, Brehmer, Louppe]  
[Karagiori, Kasieczka, Kravitz, Nachman, Shih]

- Gaining popularity in collider physics, and surpassing the wide variety of “Inference Free ML” approaches.

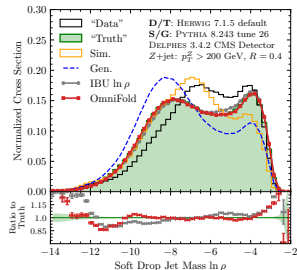
# Omnifold

- Seminal advance in unfolding for collider physics: **Omnifold**



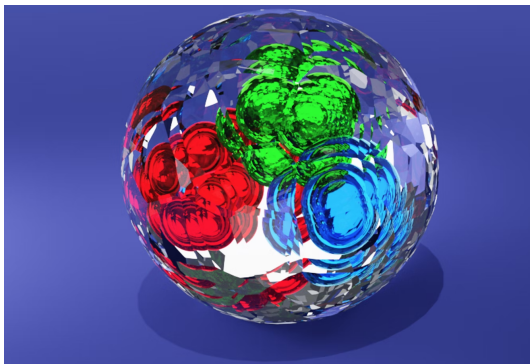
[Andreassen, Nachman]

[Andreassen, Komiske, Metodiev, Nachman, Thaler]



- Rigorously proven to reduce to Iterative Bayesian Unfolding.
- Explicit expression for likelihood intractable in high dimension  $\Rightarrow$  circumvented by classification task.
- Unfolding of qualitatively new observables (Energy Correlators), combined with theory progress  $\Rightarrow$  transformative progress in QCD.

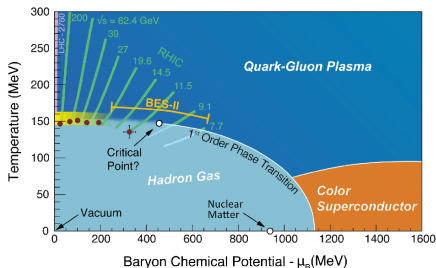
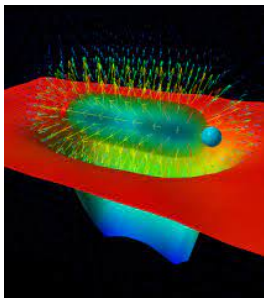
# The Frontiers of Quantum Chromodynamics





# Confinement in Quantum Chromodynamics

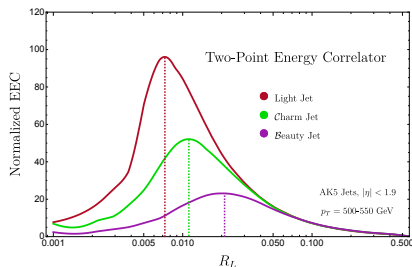
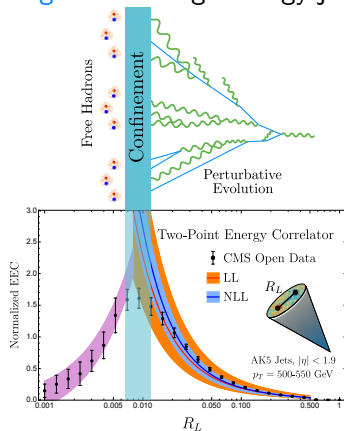
- The theory of the strong interactions is a pillar of modern physics.
- **Confinement** is one of the most important open problems in fundamental physics: **will require combined theory-experiment effort.**



- Colliders offer a **unique experimental handle on confinement** in QCD through the production of **asymptotically free quarks and gluons** in jets, or the **Quark Gluon Plasma**.

# The Confinement Transition

- Energy correlators allow the hadronization process to be directly imaged inside high energy jets.

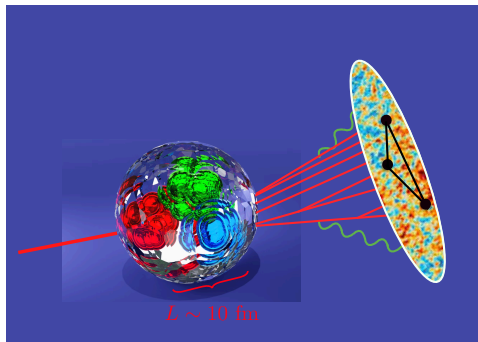
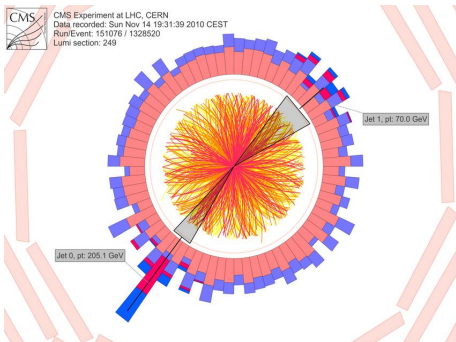


[Lee, Mecaj, Moul]

- Studying the transition for heavy mesons/baryons/onia will provide new insights into confinement.

# From Jets to Jet Substructure in Heavy Ion

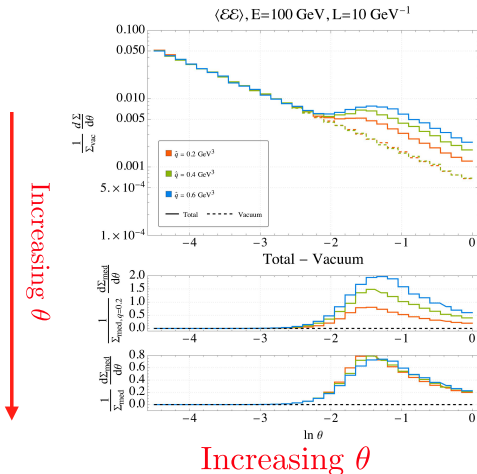
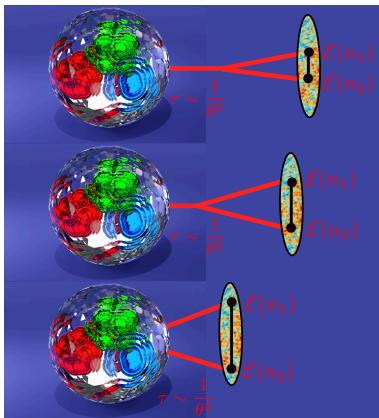
- Resolving the mystery of how asymptotically free quarks and gluons conspire to form a strongly coupled fluid is a primary goal of the heavy ion program.



- Jets are multi-scale probes  $\implies$  scales of the QGP are imprinted at characteristic scales in the substructure of jets.

# Resolving the Scales of the QGP

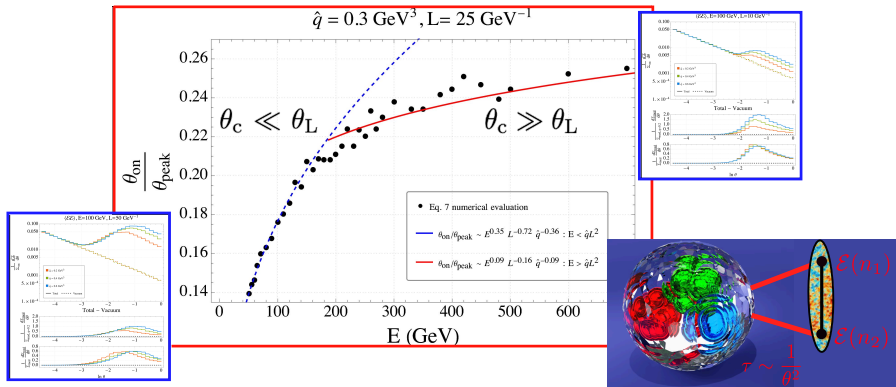
- QGP scales cleanly imprinted in two-point correlation.



[Andres, Dominguez, Holguin, Kunnawalkam Elayavalli, Marquet, Moul] →

# Resolving the Scales of the QGP

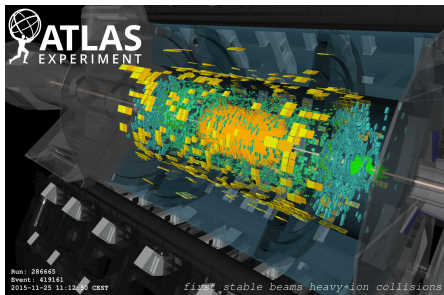
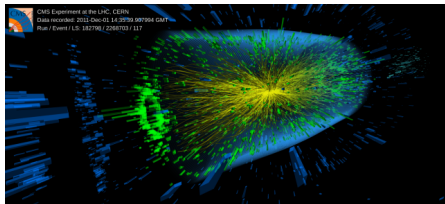
- Detailed shape of the transition can extract whether the medium interacts with the partons in the jet coherently.



- Jet Substructure provides a new lens through which to view the QGP.

# The Convergence of Heavy Ion and HEP

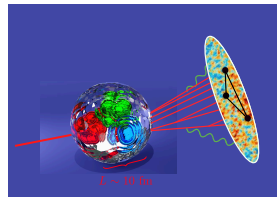
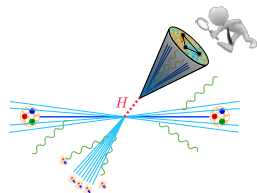
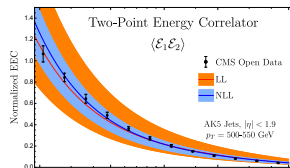
- The heavy ion programs at the LHC will continue to **blur the lines between traditional HEP and Nuclear Theory.**



- Increasing use of approaches (theory and data analysis) from HEP, with certainty for feedback into searches.
- To fully exploit this remarkable dataset for **fundamental HEP research** will require a **more synergistic approach.**

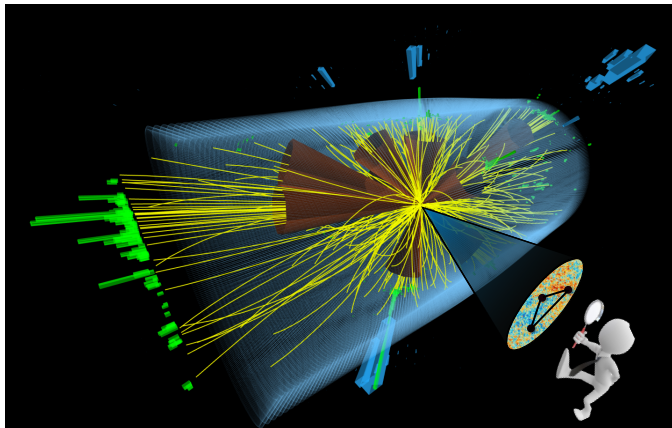
# Summary

- Formal theory has transformed **how** and **what we compute** in Jet Substructure.
- Collider physics inextricably ties **Data Science** and **Quantum Field Theory**.
- Confinement remains a pressing **open problem** in **fundamental physics** experimentally accessible only by colliders.



# Summary

- Jet Substructure continues to push the boundaries of collider physics.



- We look forward to the exciting projects from the Snowmass Process.



Thanks!